# MODIFIED FUZZY SPEED CONTROLLER OF INDUCTION MOTOR DRIVE USING EXTENDED KALMAN FILTERING

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**KEYWORDS** 

This paper focuses on application of fuzzy logic to enhance induction motor drive performance in case where the measured stator currents are distorted by Gaussian noise. For different load torques, the fixed proportional-integral (PI) speed controller provides an undesired drive performance for both transient and steady-state responses. At first, load torque is computed thanks to extended-Kalman-filtered stator currents. Next, load magnitude is employed to adjust the proportional gain and integral constant time of the fuzzy logic (FL) proportional-integral (PI) speed controller. Simulations of drive using two controllers: FL-PI and fixed PI ones, are carried out in different cases of stator current noise and load variation. Performance evaluations indicate that the FL-PI speed controller reduces the assessed indices and increases robustness to noise and load variation.

induction motor drive, proportional-integral controller, extended Kalman filter, load torque, fuzzy logic

## LIST OF ABBREVIATIONS

DTC	direct torque control
EKF	extended KF
FBR	forward braking
FL	fuzzy logic
FMO	forward motoring
FPC	fuzzy-logic PI speed controller
IM	induction motor
KF	Kalman filtering
MKF	IM-state-space-model-based EKF
PC	fixed PI speed controller
PI	proportional-integral
RBR	reverse braking
RMO	reverse motoring
SC	Signal Computation
STA	starting
SVM	space vector modulation
ULO	unloading

## **1** INTRODUCTION

Kalman filtering (KF) methods have been widely used to estimate the states or parameters of dynamical systems, such

as induction motor (IM) drive systems [Auger et al. 2013, Bose 2002]. The stator current and its time derivative are obtained using the non-IM-model-based KF for a sensorless IM drive [Brandstetter et al. 2017]. The extended KF (EKF) was associated with current derivative measurements for state and parameter estimation in synchronous reluctance motor drive [Mynar et al. 2021]. An adaptive KF technique was used to estimate the torque precisely [Stender et al. 2021].

Along with intelligent methods such as genetic algorithms and neural networks [Aissa et al. 2024, Tran et al. 2017], fuzzy logic (FL) has been widely used in engineering. The active power filter was controlled by the FL [Djendaoui et al. 2021]. To reduce the horizontal vibration of an elevator car system, the FL was combined with sliding mode control [Ge et al. 2023]. A type-2 FL system was presented to deal with rule uncertainties [Karnik et al. 1999]. To increase the reliability of the failure mode and effect analysis, the FL was integrated [Laufer 2024]. To optimize the distribution system network reconfiguration for electric vehicles, the FL was employed [Mohanty 2023]. Type-2 FL controllers were compared for their robustness to noise [Ontiveros-Robles et al. 2018]. The combination of the FL and neural network was used for diagnosis of devices such as electric drives and bearings in mechatronic systems [Peterka 2020].

In electrical drives, various FL techniques have been utilized to improve performance of fault detection, observer, controller, identification. An FL classifier was utilized to detect statorwinding faults in cage IMs [Aswad et al. 2023]. An adaptation mechanism was combined with a type-2 FL controller to ensure robustness to parameter changes at low speeds [Benlaloui et al. 2019]. Motor speed and torque were estimated by the FLbased observer [Fedor et al. 2023]. The FL systems were utilized to resolve stochastic functions in the IM drive systems [Kang et al. 2022]. Sensorless control using model reference adaptive system for permanent magnet synchronous motor (PMSM) drive was enhanced by the FL [Khanh 2022]. An adaptive FL control scheme was applied to an IM drive under load variations and disturbance [Ma et al. 2023]. The drive of a multi-motor system was implemented using state-spacerepresentation-based fuzzy model [Perdukova 2023]. The boundaries of integral time constant were adjusted to reduce the undershoot and overshoot in a proportional-integral (PI) based FL speed controller [Vo 2023b]. However, the method was based on function of speed error with coefficient tuned by trial-and-error technique. Next, the KF uses the state-space representation to obtain filtered stator currents in the case of known measurement noise. Then, the filtered currents are employed to calculate important quantities for space vector modulation-direct torque control (SVM-DTC). Finally, the calculated load torque is used to adjust boundaries of both integral time constant and proportional gain. The section structure of the paper is organized as follows: Introduction -Proposed Induction Motor Drive Structure - Simulations and Discussions - Conclusions.

# 2 PROPOSED INDUCTION MOTOR DRIVE STRUCTURE

Figure 1 shows the proposed structure using a fuzzy-logic PI speed controller (FPC) with IM-state-space-model-based extended Kalman filtering (MKF) for the SVM-direct torque controlled drive. The state-space representation of the IM is described as Eqs. (1)-(2) (Bose 2002):

$$\frac{dX}{dt} = \mathbf{A}X + \mathbf{B}U \tag{1}$$

$$Y = \mathbf{C}X\tag{2}$$

where A, B, and C: system, input, and output matrices; X, U, and Y: state, input, and output vectors. The matrices and vectors are expressed by Eqs. (3)-(8):

$$\mathbf{A} = \begin{bmatrix} a_{1} & 0 & a_{2} & a_{3}\omega_{m} \\ 0 & a_{1} & -a_{3}\omega_{m} & a_{2} \\ \frac{L_{m}R_{r}}{L_{r}} & 0 & -\frac{R_{r}}{L_{r}} & -n_{p}\omega_{m} \\ 0 & \frac{L_{m}R_{r}}{L_{r}} & n_{p}\omega_{m} & -\frac{R_{r}}{L_{r}} \end{bmatrix}$$
(3)

$$\mathbf{B} = \begin{bmatrix} \frac{1}{\sigma L_s} & 0 & 0 & 0\\ 0 & \frac{1}{\sigma L_s} & 0 & 0 \end{bmatrix}^T$$
(4)

$$\mathbf{C} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix}$$
(5)

$$\boldsymbol{X} = \begin{bmatrix} i_{s\alpha} & i_{s\beta} & \psi_{r\alpha} & \psi_{r\beta} \end{bmatrix}^T$$
(6)

$$\boldsymbol{U} = \begin{bmatrix} \boldsymbol{u}_{s\alpha} & \boldsymbol{u}_{s\beta} \end{bmatrix}^T \tag{7}$$

$$\boldsymbol{Y} = \begin{bmatrix} \boldsymbol{i}_{s\alpha} & \boldsymbol{i}_{s\beta} \end{bmatrix}^T \tag{8}$$

where:  $\omega_m$ : mechanical speed;  $n_p$ : number of pole pairs;  $L_m$ ,  $L_s$ , and  $L_r$ : magnetizing, stator, and rotor inductances;  $R_s$  and  $R_r$ : stator and rotor resistances;  $i_{s\alpha} \& i_{s\beta}$ ,  $u_{s\alpha} \& u_{s\beta}$ , and  $\psi_{r\alpha} \& \psi_{r\beta}$ two components  $\alpha$ - &  $\beta$ - of stator current, stator voltage, and rotor flux vectors in stator reference frame. The coefficients  $a_1$ ,  $a_2$ ,  $a_3$ , and  $\sigma$  are calculated according to Eqs. (9)-(12):

$$a_1 = -\frac{L_m^2 R_r + L_r^2 R_s}{\sigma L_s L_r^2}$$
(9)

$$a_2 = \frac{L_m R_r}{\sigma L_s L_r^2} \tag{10}$$

$$a_3 = \frac{n_p L_m}{\sigma L_s L_r} \tag{11}$$

$$\sigma = 1 - \frac{L_m^2}{L_s L_r} \tag{12}$$

The system described by Eqs. (1)-(2), is discretized by the Euler method. Assume that the discretized system is distorted by zero-mean, Gaussian process & measurement noise vectors v & w as Eqs. (13)-(14):

$$\boldsymbol{X}(k+1) = \boldsymbol{A}_{d}\boldsymbol{X}(k) + \boldsymbol{B}_{d}\boldsymbol{U}(k) + \boldsymbol{v}(k)$$
(13)

$$\boldsymbol{Y}(k) = \boldsymbol{C}_d \boldsymbol{X}(k) + \boldsymbol{w}(k) \tag{14}$$

where  $t_d$ : discretization period;  $A_d$ ,  $B_d$ , and  $C_d$ : system, input, and output matrices of the discretized system are computed according to Eqs. (15)-(17):

$$\mathbf{A}_d = \mathbf{I} + t_d \mathbf{A} \tag{15}$$

$$\mathbf{B}_d = t_d \mathbf{B} \tag{16}$$

$$\mathbf{C}_d = \mathbf{C} \tag{17}$$

Utilizing the discretized state-space representation of the IM, the MKF block computes the filtered stator currents  $i_{s\alpha,kf}$  and  $i_{s\beta,kf}$  according to (18) – (24) (Auger et al. 2013):

$$\tilde{\boldsymbol{X}}(k+1) = \boldsymbol{A}_d \boldsymbol{X}_{kf}(k) + \boldsymbol{B}_d \boldsymbol{U}(k)$$
(18)

$$\tilde{\mathbf{P}}(k+1) = \mathbf{A}_d(k)\hat{\mathbf{P}}(k)\mathbf{A}_d^T(k) + \mathbf{Q}$$
(19)

$$\mathbf{K}(k+1) = \tilde{\mathbf{P}}(k+1)\mathbf{C}_{d}^{T} \left[\mathbf{C}_{d}\tilde{\mathbf{P}}(k+1)\mathbf{C}_{d}^{T} + \mathbf{R}\right]^{-1}$$
(20)

$$\boldsymbol{X}_{kf}(k+1) = \tilde{\boldsymbol{X}}(k+1) + \boldsymbol{\mathrm{K}}(k+1) \Big[ \boldsymbol{Y}(k) - \tilde{\boldsymbol{Y}}(k+1) \Big]$$
(21)

$$\hat{\mathbf{P}}(k+1) = \tilde{\mathbf{P}}(k+1) - \mathbf{K}(k+1)\mathbf{C}_d\tilde{\mathbf{P}}(k+1)$$
(22)

$$\boldsymbol{Y}(k) = \boldsymbol{C}_d \boldsymbol{X}(k) \tag{23}$$

$$\tilde{\boldsymbol{Y}}(k) = \boldsymbol{C}_d \tilde{\boldsymbol{X}}(k) \tag{24}$$

where: **P**: state vector covariance matrix; **K** : Kalman gain matrix; **Q** & **R**: covariance matrices of the noise vectors v & w; symbols "~" and "^" denote predicted and estimated quantities, respectively; subscript letters "*kf*" represent Kalman-filtered ones as follows:

$$\boldsymbol{X}_{kf} = \begin{bmatrix} i_{s\alpha,kf} & i_{s\beta,kf} & \psi_{r\alpha,kf} & \psi_{r\beta,kf} \end{bmatrix}^{T}$$
(25)

The filtered stator currents are employed by the Signal Computation (SC) block to obtain essential quantities for the blocks: flux & torque controllers, vector rotation, and the FPC, according to Eqs. (26)-(31):

$$\frac{d\psi_{s\alpha,c}}{dt} = u_{s\alpha} - R_s i_{s\alpha,kf}$$
(26)

$$\frac{d\psi_{s\beta,c}}{dt} = u_{s\beta} - R_s i_{s\beta,kf}$$
(27)

$$\psi_{s,c} = \sqrt{\psi_{s\alpha,c}^2 + \psi_{s\beta,c}^2} \tag{28}$$

$$T_{e,c} = 1.5n_p \left( \psi_{s\alpha,c} i_{s\beta,kf} - \psi_{s\beta,c} i_{s\alpha,kf} \right)$$
(29)

$$\gamma_c = \sin^{-1} \left( \frac{\psi_{s\beta,c}}{\psi_{s,c}} \right) \tag{30}$$

$$T_{l,c} = T_{e,c} - J_m \frac{d\omega_m}{dt} - B_m \omega_m \tag{31}$$

where:  $J_m$  – motor inertia;  $B_m$  – rotational damping constant; subscript letter "c" presents corresponding values that are computed by the SC block including stator flux components  $\psi_{s\alpha}$ &  $\psi_{s\beta}$ , stator flux magnitude  $\psi_s$ , electromagnetic torque  $T_e$ , orienting angle  $\gamma$ , and load torque  $T_l$ .



Figure 1. The proposed IM drive structure

The FPC block shown in Fig. 2 updates the proportional gain and integral time constant according to three following steps: fuzzification, fuzzy rule base and inference engine making, and defuzzification. The two inputs of the fuzzification are the speed error  $e_{\omega}$  and its difference,  $\Delta e_{\omega}$ . The three linguistic variables, P, Z, N of the inputs denote positive, zero, and negative values, respectively, whose membership functions are described by Eqs. (32)-(37):

$$\mu_{P}(e_{\omega}) = \begin{cases}
1, & e_{\omega} \ge H_{e_{\omega}} \\
\frac{e_{\omega}}{H_{e_{\omega}}}, & 0 \le e_{\omega} < H_{e_{\omega}} \\
0, & e_{\omega} < 0 \\
0, & e_{\omega} \ge H_{e_{\omega}} \\
\frac{H_{e_{\omega}} - e_{\omega}}{H_{e_{\omega}}}, & 0 \le e_{\omega} < H_{e_{\omega}} \\
\frac{H_{e_{\omega}} + e_{\omega}}{H_{e_{\omega}}}, & -H_{e_{\omega}} \le e_{\omega} < 0 \\
0, & e_{\omega} < -H_{e_{\omega}} \\
\end{cases}$$
(32)
(32)

$$\mu_N(e_{\omega}) = \begin{cases} -\frac{e_{\omega}}{H_{e_{\omega}}}, & -H_{e_{\omega}} \le e_{\omega} < 0 \\ 1, & e_{\omega} < -H_{e_{\omega}} \end{cases}$$
(34)

$$\begin{bmatrix} 1, & \Delta e_{\omega} \ge H_{\Delta e_{\omega}} \\ \Delta e_{\omega} & \Omega \le 1 \end{bmatrix}$$

$$\mu_{P}(\Delta e_{\omega}) = \begin{cases} \frac{\Delta e_{\omega}}{H_{\Delta e_{\omega}}}, & 0 \le \Delta e_{\omega} < H_{\Delta e_{\omega}} \\ 0, & \Delta e_{\omega} < 0 \end{cases}$$
(35)

$$\Delta e_{\omega} \geq 0$$

$$\Delta e_{\omega} \geq H_{\Lambda e}$$

[0,

$$\left| \frac{H_{\Delta e_{\omega}} - \Delta e_{\omega}}{H_{\Delta e_{\omega}}}, \quad 0 \le \Delta e_{\omega} < H_{\Delta e_{\omega}} \right|$$

$$\mu_{Z}(\Delta e_{\omega}) = \begin{cases} H_{\Delta e_{\omega}} & (36) \\ \frac{H_{\Delta e_{\omega}} + \Delta e_{\omega}}{H_{\Delta e_{\omega}}}, & -H_{\Delta e_{\omega}} \leq \Delta e_{\omega} < 0 \\ 0, & \Delta e_{\omega} < -H_{\Delta e_{\omega}} \end{cases}$$

$$\begin{cases} 0, & \Delta e_{\omega} \geq 0 \\ \vdots & \vdots \end{cases}$$

$$\mu_{N}(\Delta e_{\omega}) = \begin{cases} -\frac{\Delta e_{\omega}}{H_{\Delta e_{\omega}}}, & -H_{\Delta e_{\omega}} \leq \Delta e_{\omega} < 0 \\ 1, & \Delta e_{\omega} < -H_{\Delta e_{\omega}} \end{cases}$$
(37)

where  $H_{e\omega} > 0$  and  $H_{\Delta e\omega} > 0$ . The large, medium, and small values of three linguistic variables L, M, S for two outputs, proportional gain  $K_p$  and inverse of integral time constant  $T_i$  of the defuzzification, are derived by the fuzzy rule base and inference engine shown in Tab. 1. Membership functions for L, M, S are expressed by Eqs. (38)-(43), respectively:

$$\mu_{L}(K_{p}) = \begin{cases} 1, & K_{p} \ge h_{p} \\ \frac{K_{p} - cen_{p}}{h_{p} - cen_{p}}, & cen_{p} < K_{p} < h_{p} \\ 0, & K_{p} \le cen_{p} \end{cases}$$
(38)  
$$\mu_{M}(K_{p}) = \begin{cases} 0, & K_{p} \le l_{p} \\ \frac{K_{p} - l_{p}}{cen_{p} - l_{p}}, & l_{p} < K_{p} < cen_{p} \\ \frac{h_{p} - K_{p}}{h_{p} - cen_{p}}, & cen_{p} \le K_{p} < h_{p} \\ 0, & K_{p} \ge h_{p} \\ 0, & K_{p} \ge h_{p} \end{cases}$$
(39)  
$$\mu_{S}(K_{p}) = \begin{cases} 1, & K_{p} \le l_{p} \\ \frac{cen_{p} - K_{p}}{cen_{p} - l_{p}}, & l_{p} < K_{p} < cen_{p} \\ 0, & K_{p} \ge cen_{p} \\ 0, & K_{p} \ge cen_{p} \end{cases}$$
(40)  
$$\mu_{L}(T_{i}^{-1}) = \begin{cases} 1, & T_{i}^{-1} \ge h_{i} \\ \frac{T_{i}^{-1} - cen_{i}}{h_{i} - cen_{i}}, & cen_{i} < T_{i}^{-1} < h_{i} \\ 0, & T_{i}^{-1} \le cen_{i} \end{cases}$$
(41)  
$$\mu_{M}(T_{i}^{-1}) = \begin{cases} 0, & T_{i}^{-1} \le cen_{i} \\ \frac{h_{i} - T_{i}^{-1}}{cen_{i} - l_{i}}, l_{i} < T_{i}^{-1} \le cen_{i} \\ \frac{h_{i} - T_{i}^{-1}}{cen_{i} - l_{i}}, l_{i} < T_{i}^{-1} \le h_{i} \\ 0, & T_{i}^{-1} \ge h_{i} \end{cases}$$
(42)  
$$\mu_{S}(T_{i}^{-1}) = \begin{cases} 1, & T_{i}^{-1} \le l_{i} \\ \frac{cen_{i} - T_{i}^{-1}}{cen_{i} - l_{i}}, l_{i} < T_{i}^{-1} < cen_{i} \\ 0, & T_{i}^{-1} \ge cen_{i} \end{cases}$$
(43)  
$$0, & T_{i}^{-1} \ge cen_{i} \end{cases}$$

where: boundaries of the proportional gain  $h_p \& l_p$  and the integral time constant  $h_i \& l_i$  depend on  $cen_p \& b_p$  and  $cen_i \& b_i$  according to Eqs. (44)-(45) and Eqs. (46)-(47), respectively:

$$h_p = cen_p + b_p \tag{44}$$

$$l_p = cen_p - b_p \tag{45}$$

$$h_i = \frac{1}{cen_i^{-1} - b_i} \tag{46}$$

$$l_i = \frac{1}{cen_i^{-1} + b_i} \tag{47}$$

where:  $0 < b_p < cen_p$ ;  $0 < b_i < (cen_i)^{-1}$ . The defuzzification block employs the centroid method to compute crisp values of the outputs. The magnitude of the computed load torque is limited to the range  $[-0.7T_n, 0.7T_n]$  where  $T_n$  is the rated torque. The limited value is normalized to the range  $[0, 0.7T_n]$  to obtain

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parameter  $T_{l,n}$ . The normalized value  $T_{l,n}$  is discretized using Eq. (48):

$$q = \left| 5T_{l,n} \right| + 1 \tag{48}$$

where q is an integer ranging from one to six. The parameter q is utilized to adjust the parameters of the FPC according to Eqs. (49)-(52):

$$cen_p = \frac{q+12}{10} K_{p,\text{PC}} \tag{49}$$

$$b_p = \frac{q+2}{20} K_{p,\text{PC}} \tag{50}$$

$$cen_i^{-1} = \frac{8-q}{10}T_{i,\text{PC}}$$
(51)

$$b_i = \frac{cen_i^{-1}}{10} \tag{52}$$

With this parameter update, the FPC can be considered a discontinuous type-2 fuzzy system. Parameters surfaces of the FPC in cases of q = 1, and q = 6 are shown in Figs. 3-4. The axes of variables  $e_{\omega}$  and  $\Delta e_{\omega}$  in the figures are divided by  $\omega_{m,ref}$ .



Figure 2. Fuzzy logic PI speed controller

	<i>e</i> <sub>@</sub>				
Δe <sub>ø</sub>	Р	Ζ	N		
Р	<i>L</i> , <i>S</i>	<i>M</i> , <i>S</i>	<i>S</i> , <i>S</i>		
Ζ	<i>L, М</i>	М, М	<i>S</i> , <i>M</i>		
N	<i>L</i> , <i>L</i>	М, L	<i>S</i> , <i>L</i>		

Table 1. Fuzzy rule base and inference engine

## **3** SIMULATIONS AND DISCUSSIONS

Drives utilizing two speed controllers, fixed PI speed controller (PC) and the FPC, are implemented in Matlab/Simulink environment at reference mechanical speeds of  $\pi$  (rad/s) and  $10\pi$  (rad/s), load torques of  $0.1T_n$  and  $0.7T_n$ , and variance  $\delta^2$  of stator current measurement noise of  $0.25^2$  and  $1.0^2$ . Tables 2 and 3 show the parameters of the IM and drive, respectively. In time courses, there are 6 durations: 0.0s-0.5s, 0.5s-0.9s, 0.9s-1.3s, 1.3s-2.4s, 2.4s-2.7s, and 2.7s-3.0s, corresponding to 6 operations of the IM drive including starting (STA), forward motoring (FMO), forward braking (FBR), reverse motoring (RMO), reverse braking (RBR), and unloading (ULO) [Vo 2023a].



**Figure 3.** Parameters surface of the FPC:  $K_p$  (upper) and  $T_i^{-1}$ , case q = 1



**Figure 4.** Parameters surface of the FPC:  $K_p$  (upper) and  $T_i^{-1}$ , case q = 6

Parameter	Value	Parameter	Value
Rated power	2.2kW	Motor inertia	0.0047kg.m <sup>2</sup>
Rated	14N.m	Mutual	0.192H

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torque		inductance	
Rated voltage	230V/400V	Stator/rotor inductance	0.209H
Rated speed	1420rpm	Stator resistance	3.179Ω
Number of pole pairs	2	Rotor resistance	2.118Ω

**Table 2.** The motor parameters [Vo 2023a]

Block	Parameter	Value
Speed controller	Proportional gain K <sub>p,PC</sub>	1.5
	Integral time constant Ti,PC	0.05s
	Output limits	±14N.m
Flux Proportional gain		100
controller	Integral time constant	0.01s
Torque	Proportional gain	5
controller	Integral time constant	0.05s
Voltage	DC link voltage	540V
source	Switching frequency	4kHz
inverter	Modulation technique	SVM

**Table 3.** The drive parameters [Vo 2023a]

Figures 5-12 show mechanical speed responses for listed cases of noise variance, load torque, and reference mechanical speed. Through enlarged images shown in the figures, it is easy to see that the speed response of the FPC has lower overshoot/undershoot than that of the PC. For more detail, overshoot/undershoot is displayed in Tabs. 4-9 corresponding to IM operations. For the starting (see Tab. 4) , the FPC overshoot is reduced by at most 61% compared to the PC one at  $\omega_{m,ref} = \pi$ ,  $\partial^2 = 1^2$ . For the FMO, FBR and RBR operations (see Tabs. 5, 6 and 8), the cases where FPC's overshoot decreases the most compared to PC's occur at the highest load torque. Cases of the RMO and ULO operations (see Tabs. 7 and 9), the greatest reduction in FPC overshoot compared to PC overshoot is achieved at maximum load or maximum noise variance. In order to compare the performance at steady state of two speed controllers, the ripple calculated during last 0.1 second of each drive operation, is listed in Tabs. 10-15.







Figure 6. Speeds at  $\omega_{m,ref} = \pi$  (rad/s),  $T_l = 0.1T_n$ ,  $\delta^2 = 1.0^2$ 



**Figure 7.** Speeds at  $\omega_{m,ref} = \pi$  (rad/s),  $T_l = 0.7T_n$ ,  $\delta^2 = 0.25^2$ 

In Tab. 10, the ripple for the STA operation of the FPC is decreased by at most 48% compared to that of the PC at  $\omega_{m,ref}$ =  $10\pi$ ,  $\delta^2 = 1^2$ . For the five remaining operations (Tabs. 11-15), the FPC ripple is increasingly reduced compared to the PC ripple as the noise variance increases. Figures 13-14 show the speed responses at  $\omega_{m,ref} = \{\pi, 10\pi\}, T_l = 0.7T_n, \partial^2 = 2^2$ . They indicated that the FPC is much more robust than the PC in the case of large noise variances and the highest load torque. In particular, the PC cannot track the reference signal during the RMO operation (see blue waveform in Fig. 14). The filtered stator current responses at  $\omega_{m,ref} = \{\pi, 10\pi\}, T_l = 0.7T_n, \partial^2 = \{1^2, \dots, n\}$ 2<sup>2</sup>} are displayed in Figs. 15-18. Although currents are smoothed by the MKF, they tend to deviate from the sine wave shape as the noise variance increases, particularly for the PC. The parameter q shown in Figs. 19-20 indicates that as variance  $\delta^{\!2}$  increases, the calculated load torque fluctuates.







**Figure 9.** Speeds at  $\omega_{m,ref} = 10\pi$  (rad/s),  $T_l = 0.1T_n$ ,  $\partial^2 = 0.25^2$ 



**Figure 10.** Speeds at  $\omega_{m,ref} = 10\pi$  (rad/s),  $T_l = 0.1T_n$ ,  $\delta^2 = 1.0^2$ 



**Figure 11.** Speeds at  $\omega_{m,ref} = 10\pi$  (rad/s),  $T_l = 0.7T_n$ ,  $\delta^2 = 0.25^2$ 



**Figure 12.** Speeds at  $\omega_{m,ref} = 10\pi$  (rad/s),  $T_l = 0.7T_n$ ,  $\delta^2 = 1.0^2$ 

		82					
Øm,ref	0.2	25 <sup>2</sup>	1.0 <sup>2</sup>				
	PC	FPC	PC	FPC			
π	1.63	1.76	5.57	2.12			
10π	0.16	0.16	0.37	0.20			

Table 4. Overshoot (%) at STA operation

		8			
Øm,ref	T∥Tn	0.25 <sup>2</sup>		1.0 <sup>2</sup>	
		PC	FPC	PC	FPC

_	0.1	3.81	3.05	5.31	4.16
л	0.7	21.2	11.2	21.8	12.6
10-	0.1	0.37	0.33	0.51	0.34
TON	0.7	2.21	1.21	2.03	1.19

Table 5. Undershoot (%) at FMO operation

Øm,ref		8				
	T∥Tn	0.25 <sup>2</sup>		1.0 <sup>2</sup>		
		PC	FPC	PC	FPC	
-	0.1	7.23	6.41	6.65	6.66	
π	0.7	41.9	24.3	44.0	23.9	
10	0.1	0.69	0.54	0.78	0.56	
τΟπ	0.7	4.14	2.33	4.04	2.31	

Table 6. Overshoot (%) at FBR operation

Øm,ref		8				
	T∥Tn	0.25 <sup>2</sup>		1.0 <sup>2</sup>		
		PC	FPC	PC	FPC	
π	0.1	1.87	1.73	5.82	2.17	
	0.7	2.14	1.70	6.04	1.88	
10-	0.1	0.18	0.16	0.61	0.21	
TON	0.7	0.17	0.17	0.43	0.19	

Table 7. Overshoot (%) at RMO operation

Øm,ref		8				
	T∥Tn	0.25 <sup>2</sup>		1.0 <sup>2</sup>		
		PC	FPC	PC	FPC	
π	0.1	7.41	6.00	8.17	5.54	
	0.7	41.7	21.7	41.2	21.6	
10-	0.1	0.69	0.58	0.80	0.53	
TOR	0.7	4.11	2.31	3.96	2.25	

Table 8. Overshoot (%) at RBR operation

Øm,ref		8				
	T∥Tn	0.25 <sup>2</sup>		1.0 <sup>2</sup>		
		PC	FPC	PC	FPC	
π	0.1	4.24	3.34	5.42	3.00	
	0.7	22.3	13.0	22.1	13.3	
10-	0.1	0.44	0.32	0.60	0.33	
TON	0.7	2.10	1.29	2.09	1.26	

Table 9. Undershoot (%) at ULO operation

Øm,ref	F					
	0.2	25 <sup>2</sup>	1.0 <sup>2</sup>			
	PC	FPC	PC	FPC		
π	2.72	2.65	3.91	3.88		
10π	0.35	0.33	0.75	0.39		

Table 10. Ripple (%) at STA operation

			8 <sup>2</sup>			
Øm,ref	T∥Tn	0.25 <sup>2</sup>		1.0 <sup>2</sup>		
		PC	FPC	PC	FPC	
π	0.1	2.49	2.75	5.26	3.60	

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	0.7	3.02	2.82	7.89	2.90
10π	0.1	0.31	0.31	0.93	0.32
	0.7	0.33	0.35	0.87	0.34

Table 11. Ripple (%) at FMO operation

			$\delta^2$				
	Øm,ref	T∥Tn	0.25 <sup>2</sup>		1.0 <sup>2</sup>		
			PC	FPC	PC	FPC	
	π	0.1	2.95	3.44	8.97	3.61	
		0.7	3.15	2.73	6.93	3.20	
	10π	0.1	0.33	0.29	0.84	0.36	
		0.7	0.18	0.18	0.50	0.17	

Table 12. Ripple (%) at FBR operation

			8 <sup>2</sup>				
Øm,ref	T∥Tn	0.2	25 <sup>2</sup>	1.0 <sup>2</sup>			
		PC	FPC	PC	FPC		
_	0.1	3.11	2.74	6.93	3.52		
n	0.7	3.26	3.05	6.96	2.96		
10-	0.1	0.31	0.34	0.55	0.33		
TON	0.7	0.45	0.33	0.95	0.38		

Table 13. Ripple (%) at RMO operation

			8 <sup>2</sup>				
	Øm,ref	T∥Tn	0.25 <sup>2</sup>		1.0 <sup>2</sup>		
			PC	FPC	PC	FPC	
	π	0.1	2.89	2.79	8.43	4.23	
		0.7	2.90	2.98	8.53	2.69	
	10-	0.1	0.32	0.29	0.84	0.35	
	IOn	0.7	0.32	0.29	0.64	0.31	

Table 14. Ripple (%) at RBR operation

			82				
	Øm,ref	T∥Tn	0.25 <sup>2</sup>		1.0 <sup>2</sup>		
			PC	FPC	PC	FPC	
	_	0.1	3.04	2.74	8.83	3.86	
	n	0.7	2.82	2.88	6.50	3.98	
	10-	0.1	0.32	0.32	0.71	0.35	
	IOn	0.7	0.33	0.30	0.70	0.37	

Table 15. Ripple (%) at ULO operation



**Figure 13.** Speeds at  $\omega_{m,ref} = \pi$  (rad/s),  $T_l = 0.7T_n$ ,  $\partial^2 = 2.0^2$ 



**Figure 14.** Speeds at  $\omega_{m,ref} = 10\pi$  (rad/s),  $T_l = 0.7T_n$ ,  $\delta^2 = 2.0^2$ 



**Figure 15.** Currents at  $\omega_{m,ref} = \pi$  (rad/s),  $T_l = 0.7T_n$ ,  $\delta^2 = 1.0^2$ 











**Figure 18.** Currents at  $\omega_{m,ref} = 10\pi$  (rad/s),  $T_l = 0.7T_n$ ,  $\partial^2 = 2.0^2$ 



**Figure 19.** Parameter *q* at  $\omega_{m,ref} = \pi$  (rad/s),  $T_l = 0.7T_n$ ,  $\delta^2 = \{1.0^2, 2.0^2\}$ 



**Figure 20.** Parameter *q* at  $\omega_{m,ref} = 10\pi$  (rad/s),  $T_l = 0.7T_n$ ,  $\partial^2 = \{1.0^2, 2.0^2\}$ 

### 4 CONCLUSIONS

A drive structure using IM-model-based extended Kalman filtering integrated with a PI speed controller, whose parameters were updated by fuzzy logic according to the computed load torque, was presented. The structure and the one with a fixed-parameter PI speed controller were simulated in different cases of reference mechanical speed, load torque, and known measurement stator current noise covariance. The structure with the FPC significantly improved both the transient and steady-state speed responses compared with the structure with the PC, especially up to 69% and 63% reductions in overshoot/undershoot and ripple at very-low reference mechanical speed and high load torque. In addition, it offered much strong robustness than the one with PC, even in cases of large noise variance. The proposed structure can be used for sensorless IM drives. Adaptive Kalman filtering techniques can be used to obtain more precise information on the load torque magnitude. The FL techniques can be deployed to identify IM parameters. Type-2 or type-3 fuzzy logic can be developed to achieve greater robustness to large variations in disturbance and load torque.

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